

# From Flying Bees to Autonomous Robots

M.V. Srinivasan, J.S. Chahl and S.W. Zhang

Centre for Visual Science  
Research School of Biological Sciences  
Australian National University



“Srini” Srinivasan



# Peculiarities of insect vision

Small interocular separation

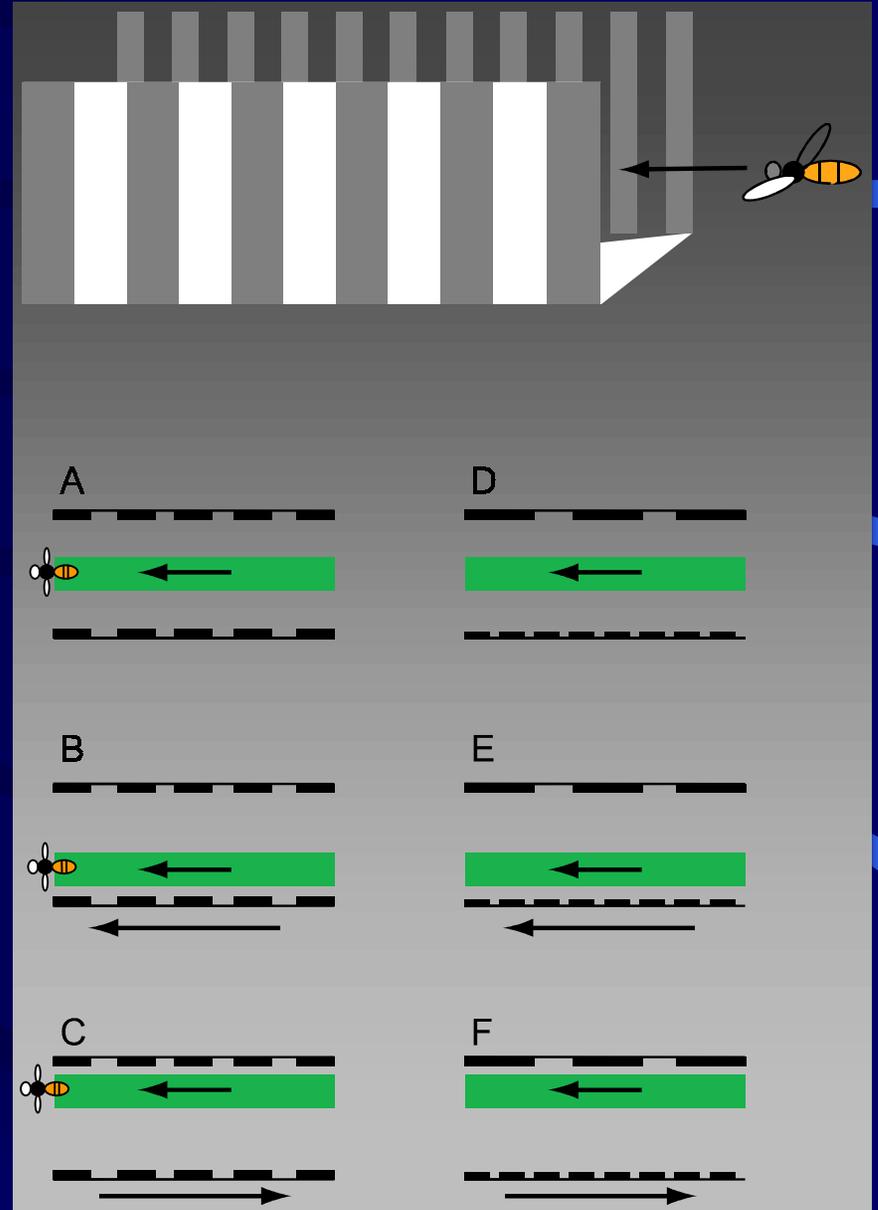
Therefore, stereo vision is difficult



Insects rely heavily on image motion cues to infer object distance, perceive the world in 3-D and navigate in it



# Bees negotiate narrow gaps by balancing the image velocities in the two eyes



Kirchner & Srinivasan  
*Naturwissenschaften* (1988)

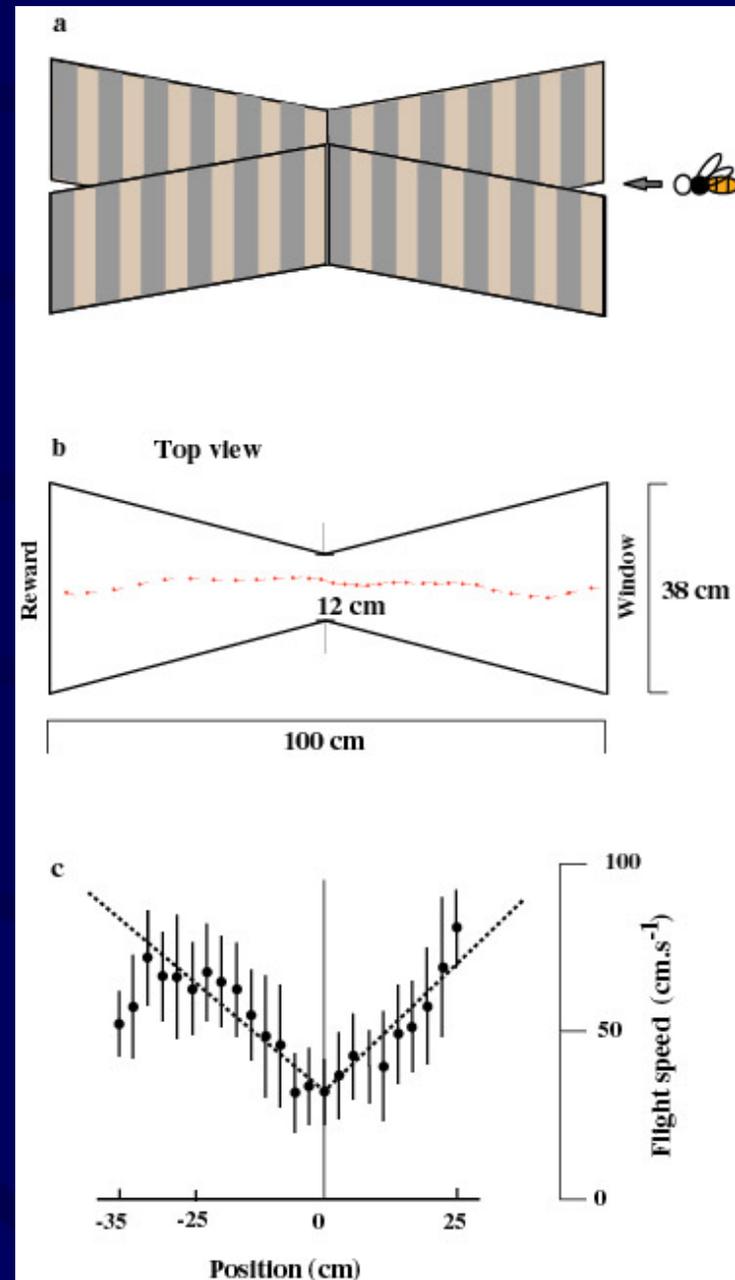
Srinivasan, Lehrer, Kirchner & Zhang  
*Vis. Neurosci.* (1991)

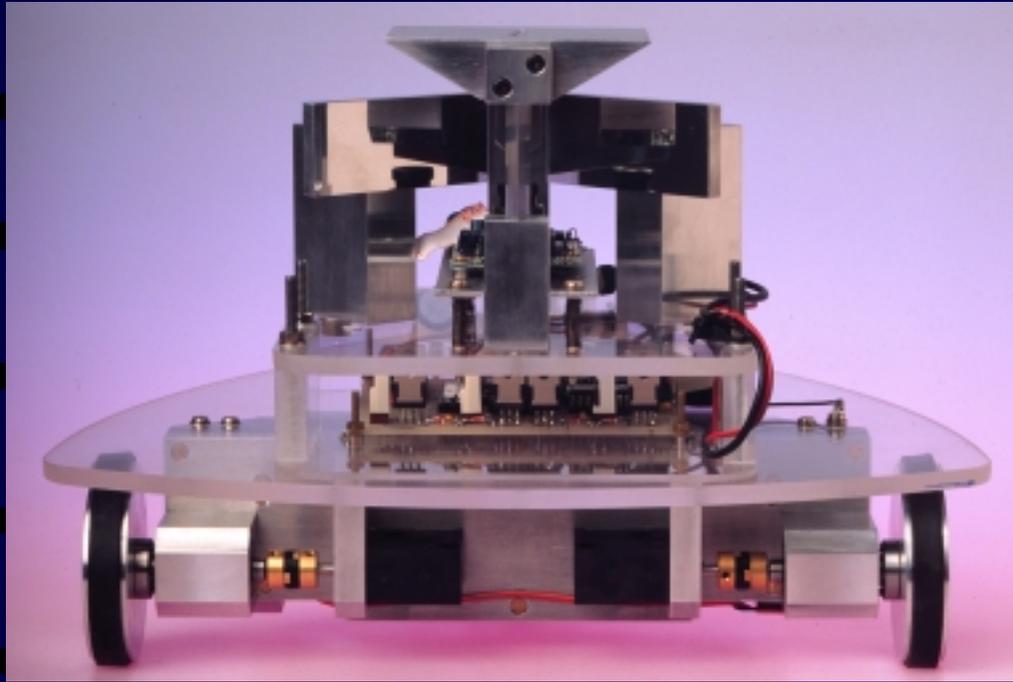


# Control of flight speed

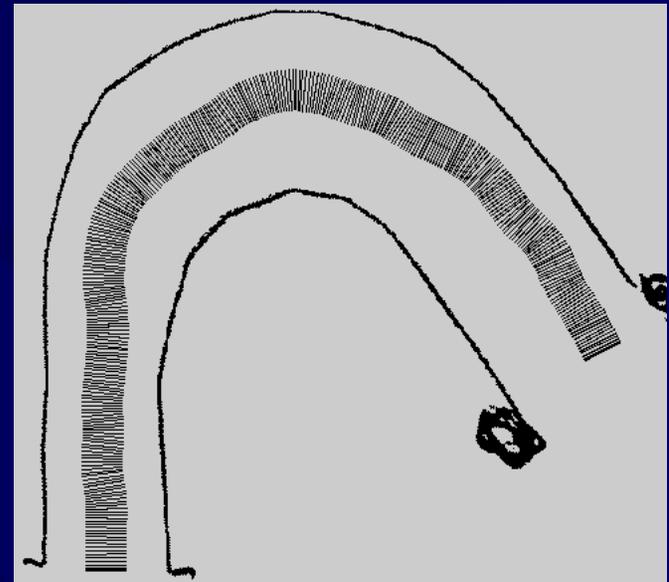
Speed of flight is regulated by holding the global image velocity constant

Srinivasan, Zhang, Lehrer & Collett  
*J. Exp. Biol.* (1996)





This robot, about the size of a skateboard, navigates along corridors by balancing optic flows on the left and the right



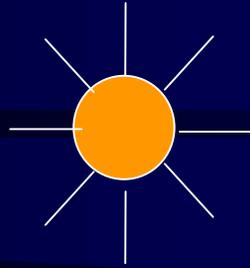
Weber, Chahl, Srinivasan & Venkatesh (1997)

# Landing

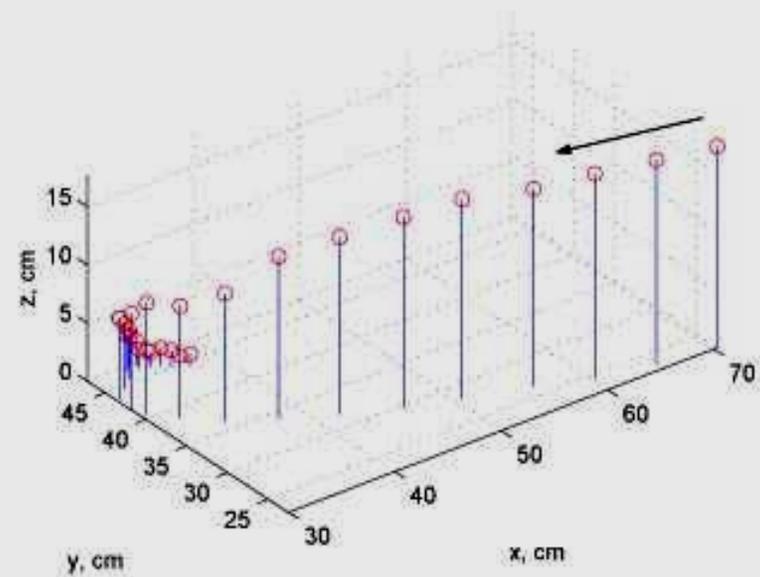
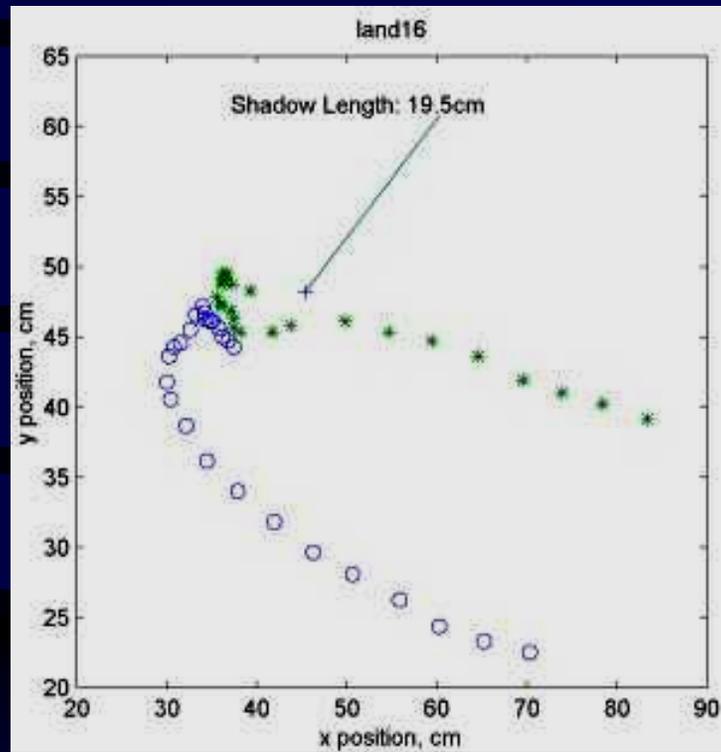


How does a bee perform a smooth, grazing landing on a horizontal surface ?

# Filming trajectories of landing bees



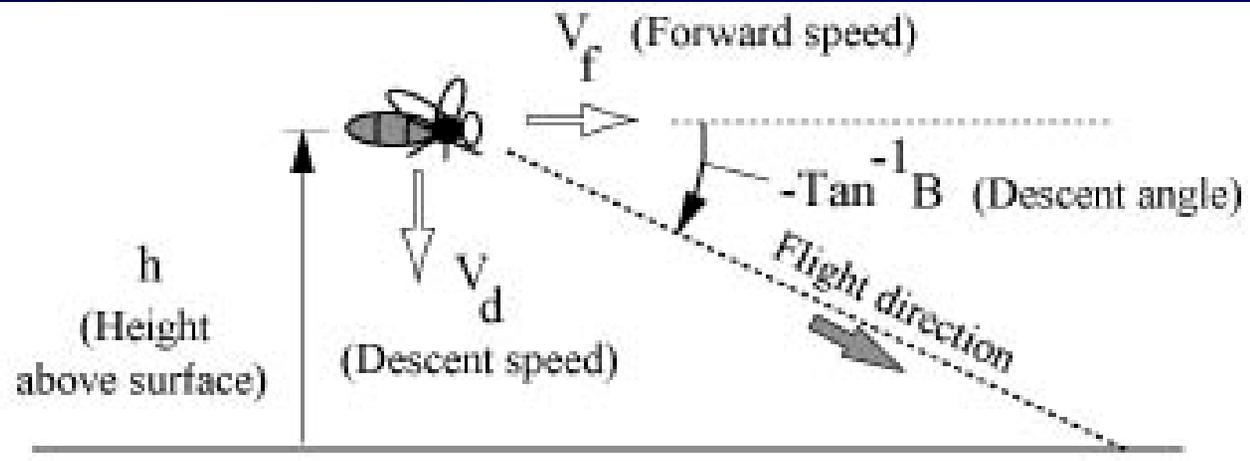
# Reconstruction of landing trajectories in 3d



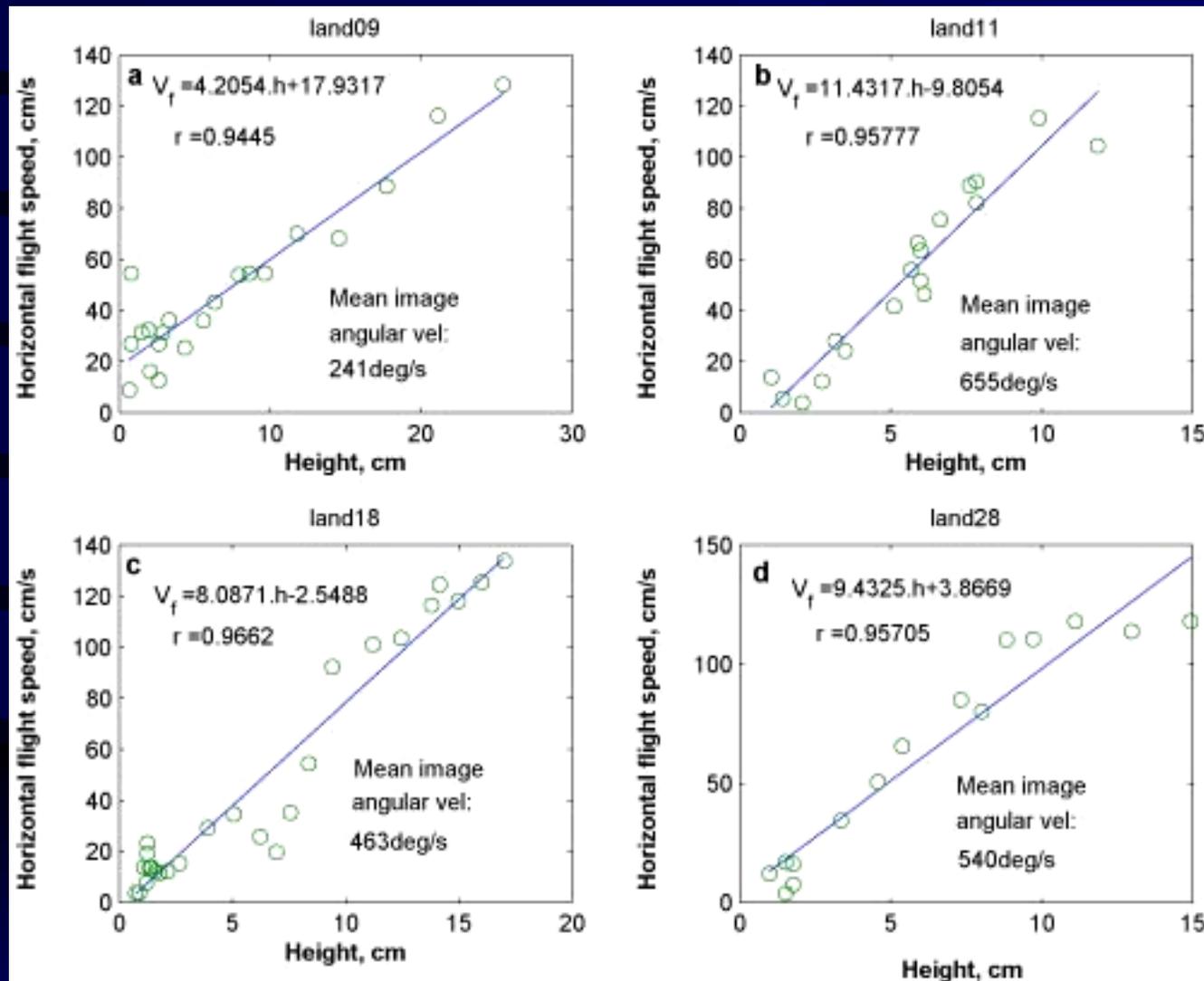
Srinivasan, Zhang, Chahl, Barth & Venkatesh  
*Biol. Cybern.* (2000)



# Landing parameters



# Horizontal flight speed versus height



Srinivasan, Zhang, Chahl, Barth & Venkatesh, *Biol. Cybern* (2000)



# Rules for landing

1. Ground image speed is held constant

$$V_f(t) = \omega \cdot h(t)$$

2. Instantaneous descent speed  $V_d(t)$  is coupled to instantaneous forward flight speed  $V_f(t)$ :

$$V_d(t) = -\frac{dh(t)}{dt} = B \cdot V_f(t)$$



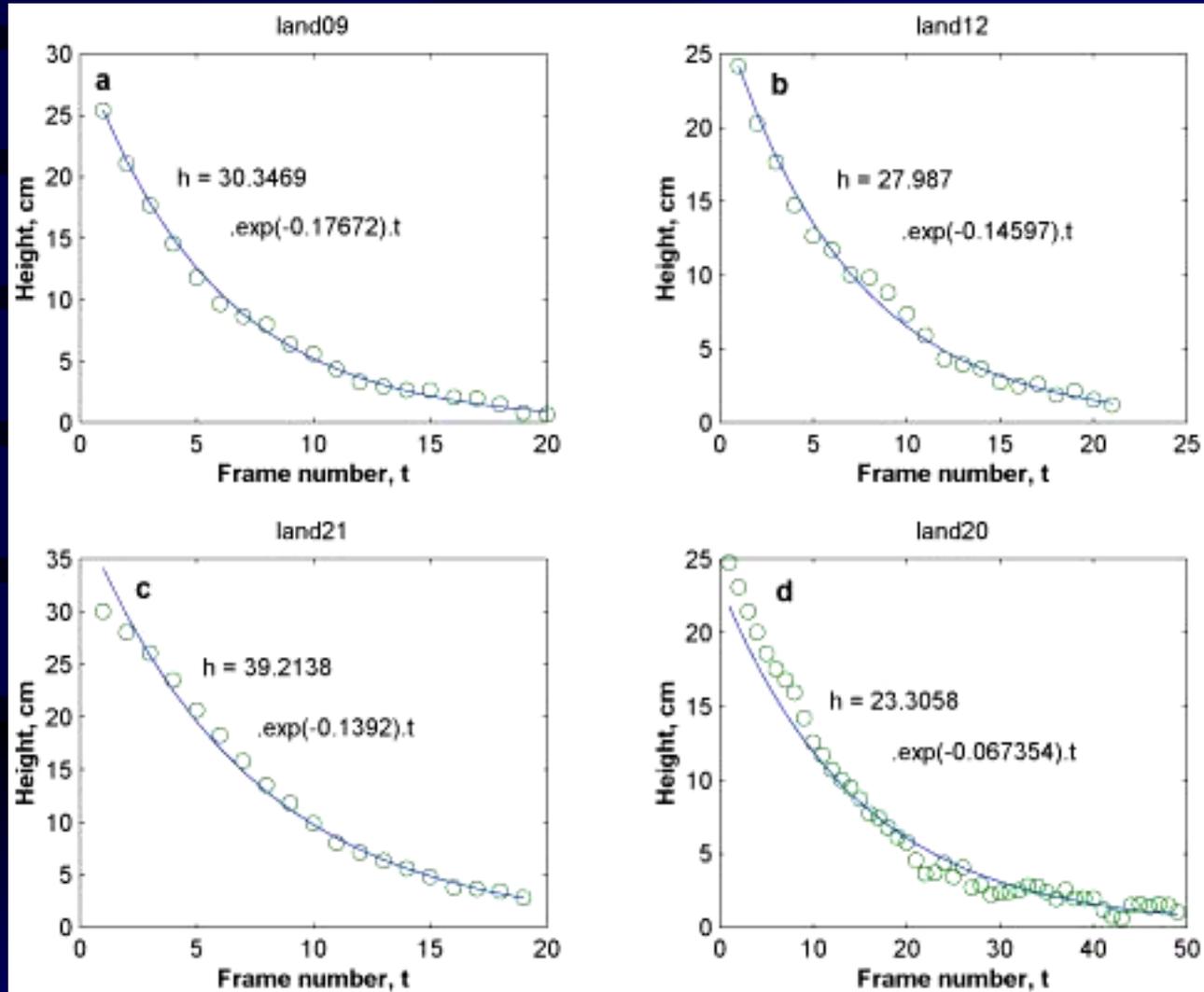
Model prediction 1:

$$h(t) = h(t_0) \cdot e^{-\omega \cdot B \cdot t}$$

⇒ Height decreases exponentially with time



# Test of prediction 1



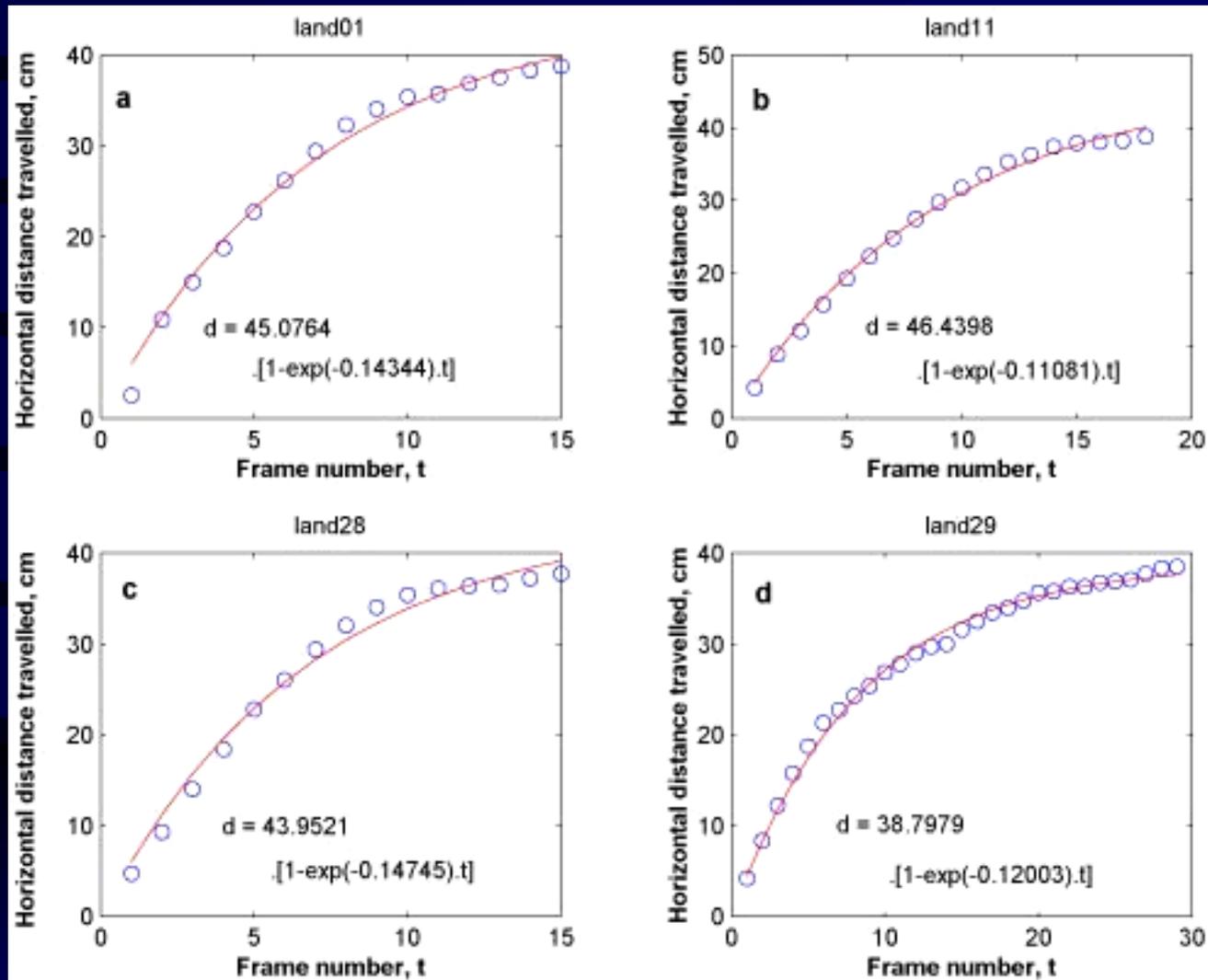
## Model prediction 2:

$$Hordist = \frac{h(t_0)}{B} \cdot [1 - e^{-\omega \cdot B \cdot t}]$$

⇒ Cumulative horizontal distance travelled is a saturating exponential function of time



# Test of Prediction 2



Srinivasan, Zhang, Chahl, Barth & Venkatesh, *Biol. Cybern* (2000)





# Test of landing algorithm on a gantry robot

← Computer-controlled gantry  
with panoramic vision head



Panoramic  
image



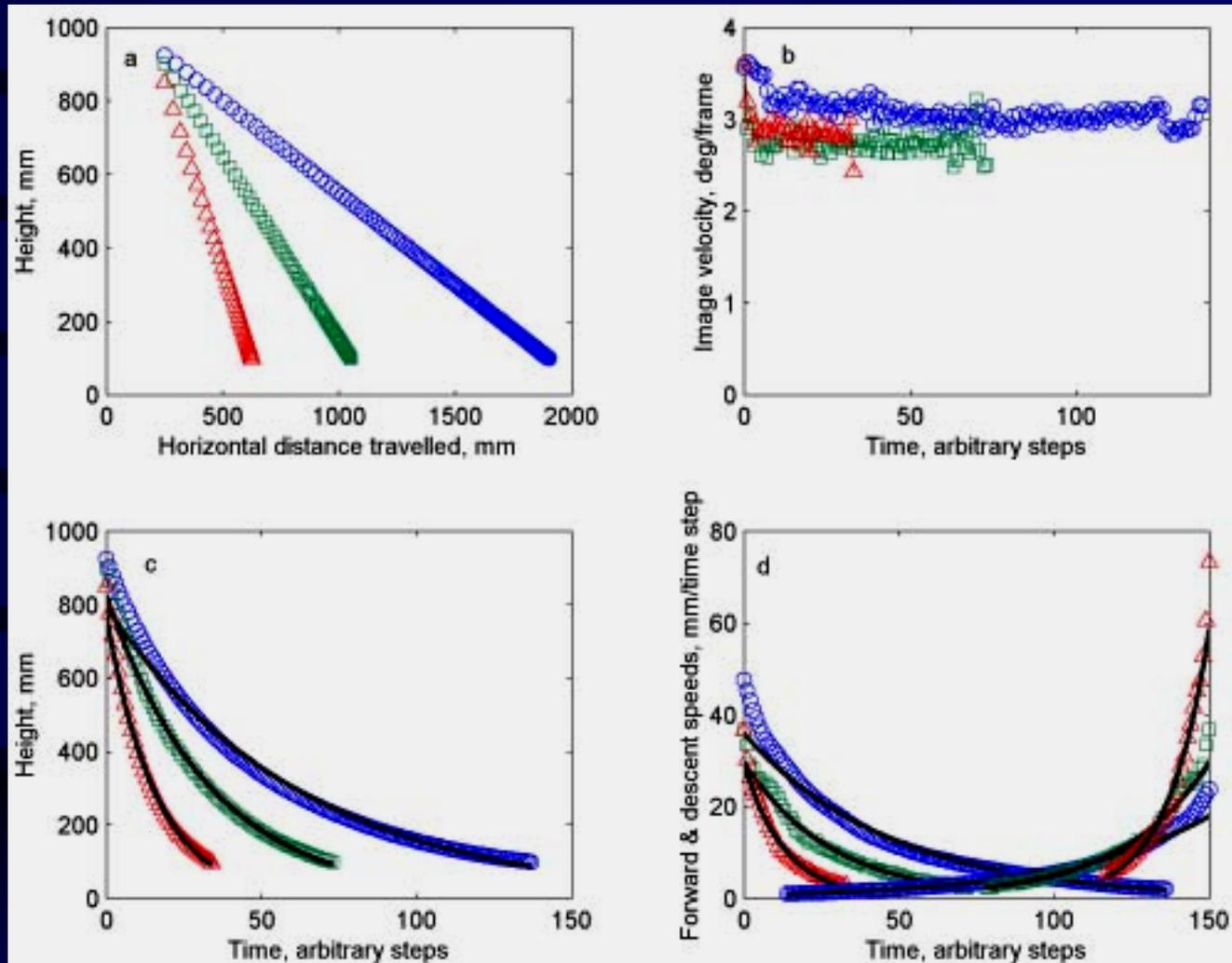
X flow



Y flow



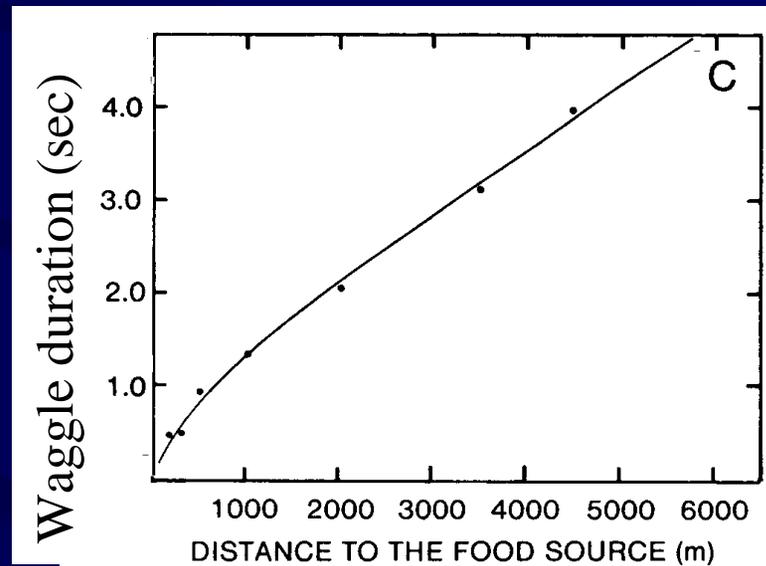
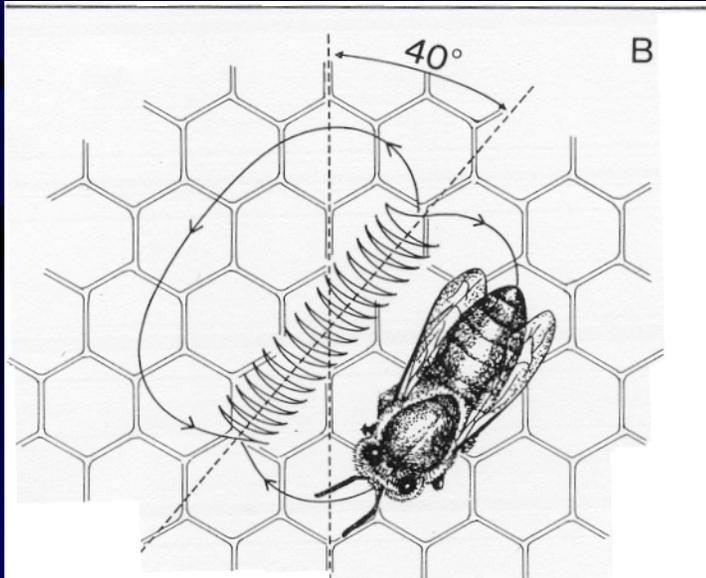
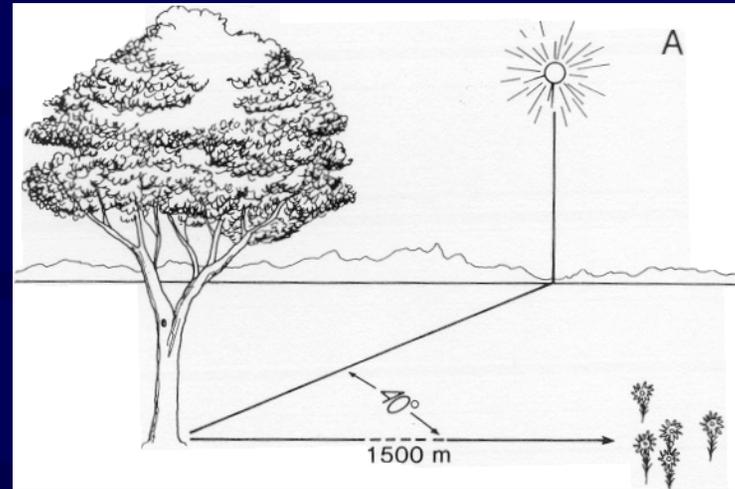
# Gantry experiments: results



Srinivasan, Zhang, Chahl, Barth & Venkatesh, *Biol. Cybern.* (2000)

# Honeybee odometry

## The waggle dance



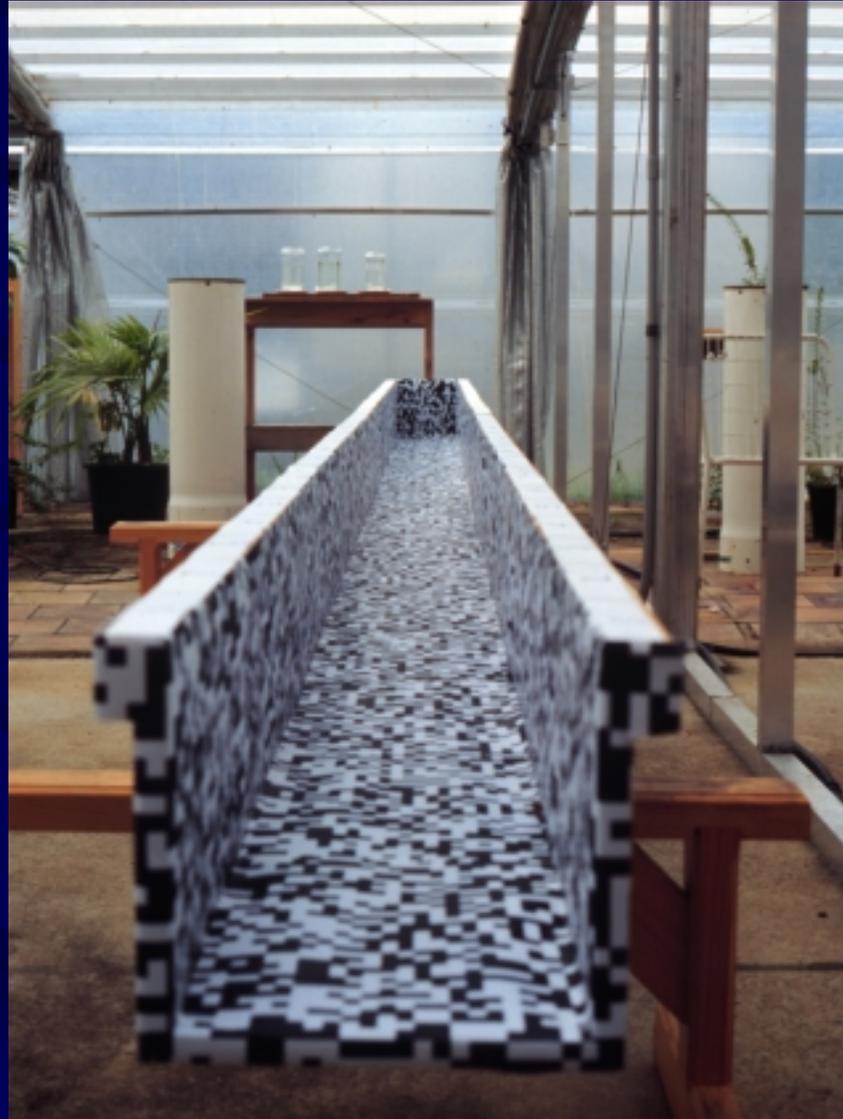
Q: How does a bee work out how far she has flown?

## AWBFF: All-Weather Bee Flight Facility



## Honeybee odometry

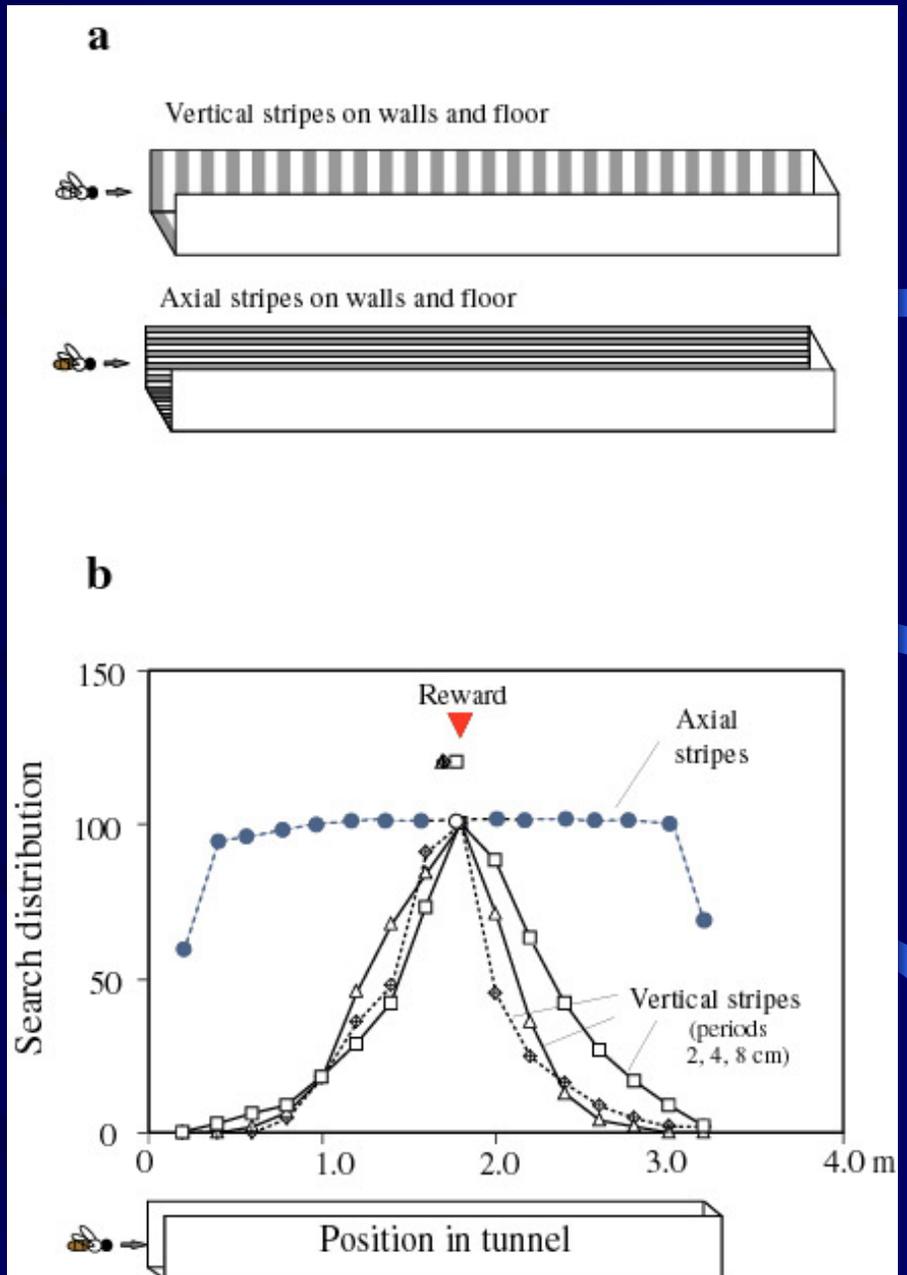
Bees are trained to find a food source placed at a fixed location inside a tunnel lined with a visual texture

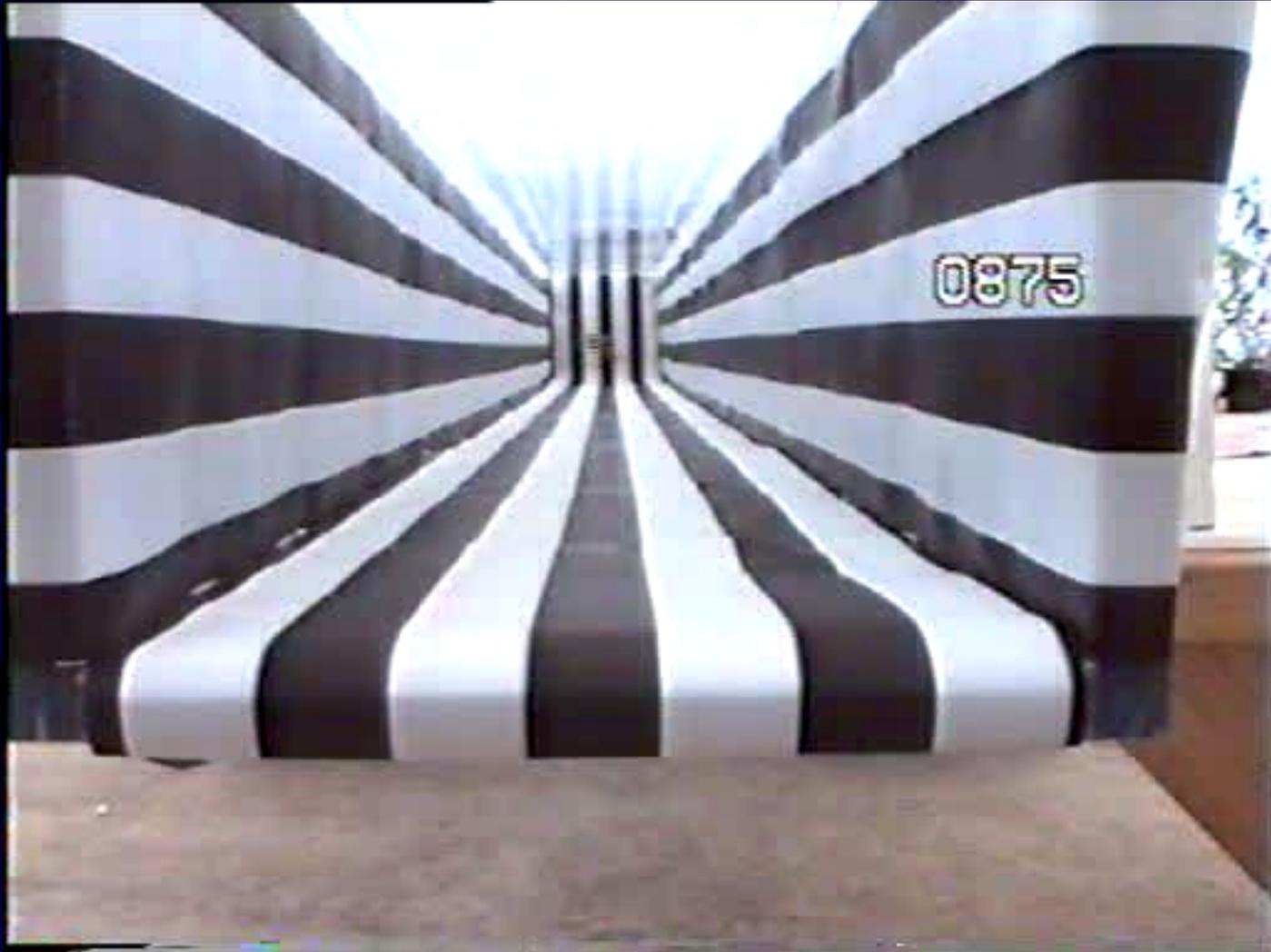


# Honeybee odometry

Bees can learn the location of a food source placed inside a tunnel lined with vertical stripes

They *cannot* learn the location if the tunnel is lined with horizontal stripes





# Honeybee navigation: What is the nature of the odometer?



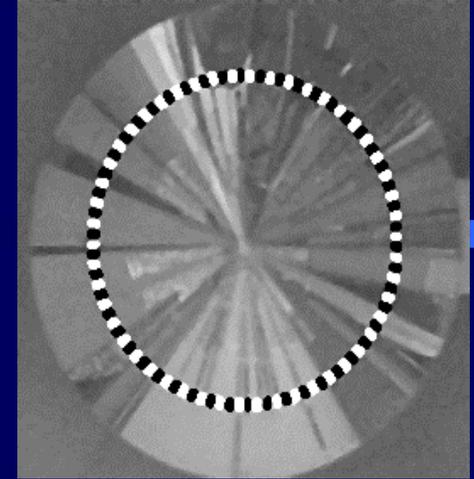
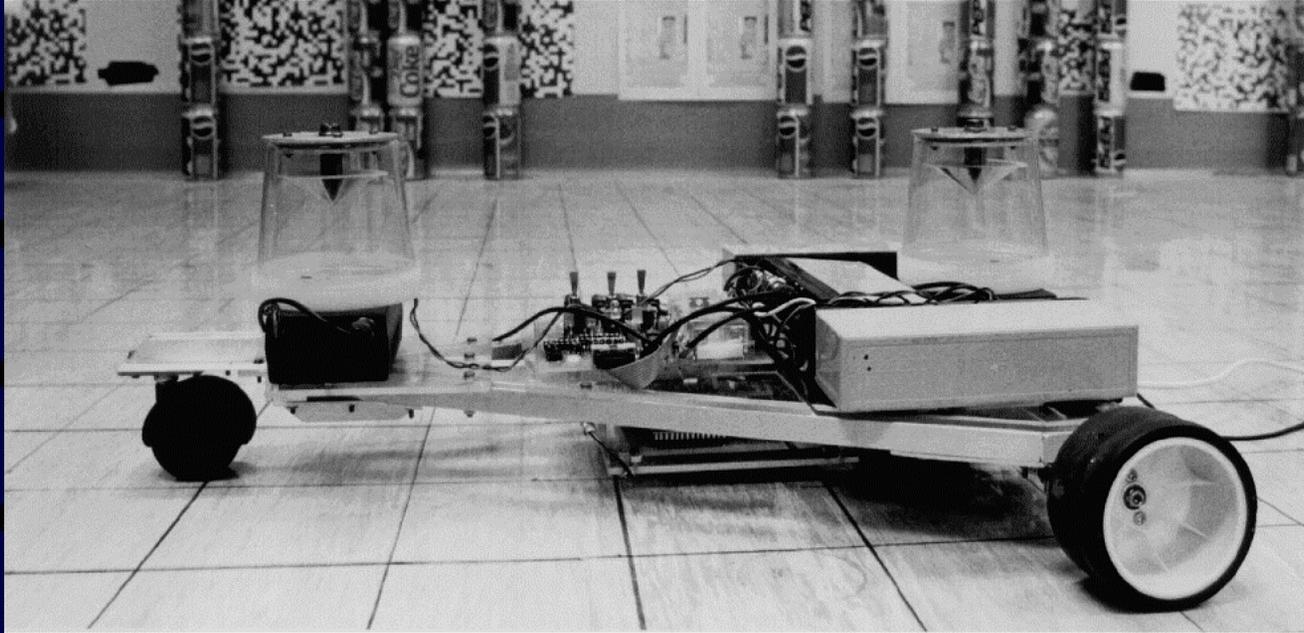
Landmark count  
Time of flight  
Wingbeat count  
Energy consumption

Airspeed integration  
Inertial navigation

Integration of optic flow



# Egomotion computing robot

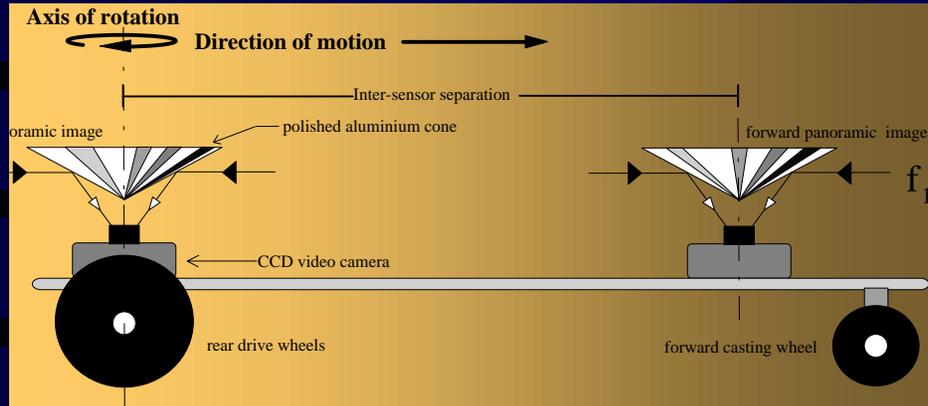


This robot, about the size of a skateboard, estimates its motion through the environment by integrating optic flow (or, more accurately, image deformation)

It requires no prior knowledge of the environment



Chahl & Srinivasan, *Biol. Cybernetics* (1996)



$$\hat{f}(\theta) \cong (1 - \alpha)f_0(\theta) + \alpha f_1(\theta) \quad (1)$$

We minimise the mean square error between  $f(\theta)$  and  $\hat{f}(\theta)$ . That is, we minimise

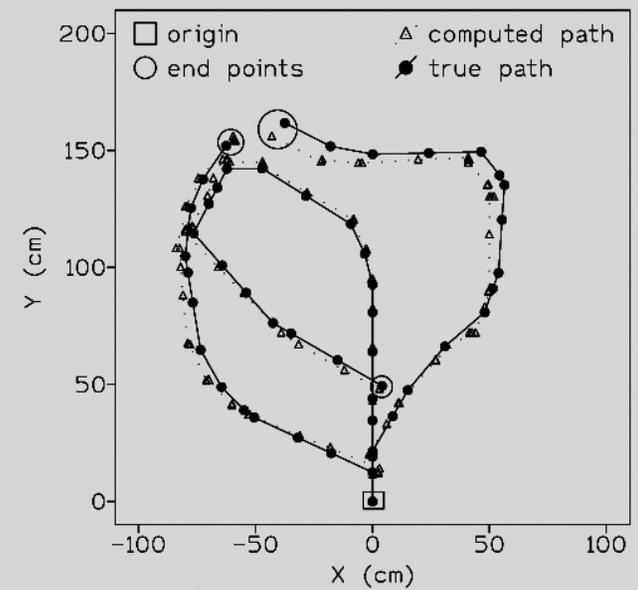
$$\int_0^{2\pi} \left[ \{(1 - \alpha)f_0(\theta) + \alpha f_1(\theta)\} - f(\theta) \right]^2 d\theta \quad (2)$$

with respect to  $\alpha$ .

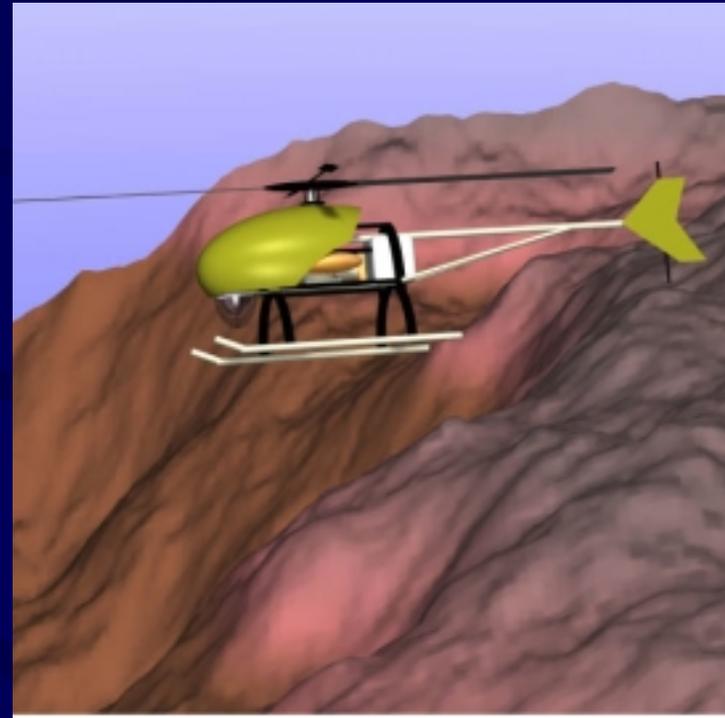
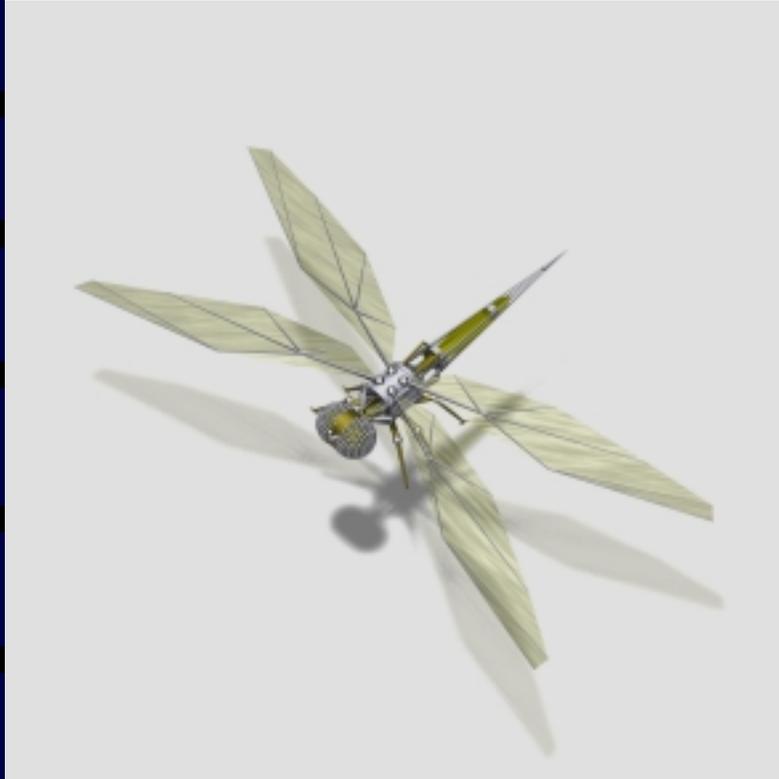
This minimisation yields

$$\alpha = \frac{\int_0^{2\pi} [f(\theta) - f_0(\theta)] [f_1(\theta) - f_0(\theta)] d\theta}{\int_0^{2\pi} [f_0(\theta) - f_1(\theta)]^2 d\theta} \quad (3)$$

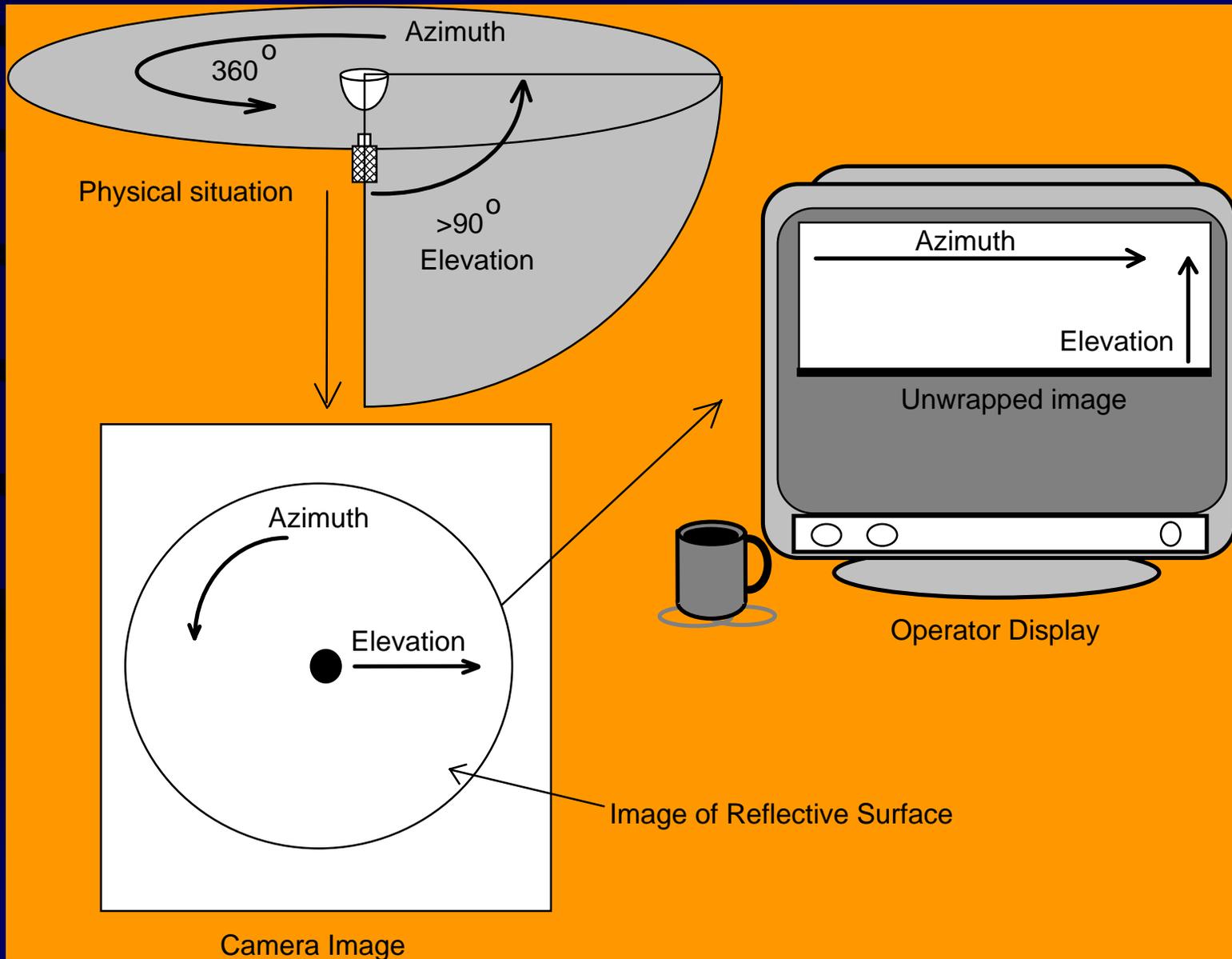
Since  $f_0(\theta)$ ,  $f(\theta)$  and  $f_1(\theta)$  are known,  $\alpha$  is readily computed.



## Flying machines



# Panoramic Imaging System



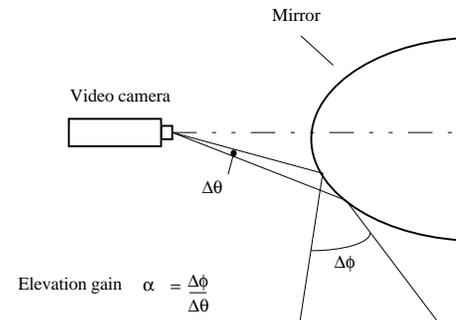
The system comprises a standard video camera viewing a specially shaped reflective surface. The surface has the property that a given change in the angular elevation of view in the external environment maps to a constant radial displacement in the camera's image



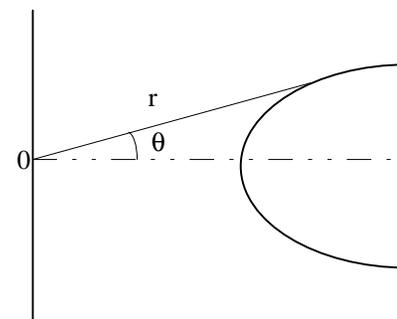
Constraint equation for generating profile of panoramic imaging surface



Chahl & Srinivasan, *J. Opt. Soc. Am. A* (1997)



**Figure 1**  
Camera-mirror configuration, illustrating the elevation gain  $\alpha$ .



**Figure 2**  
Polar co-ordinate system for definition of mirror profile.

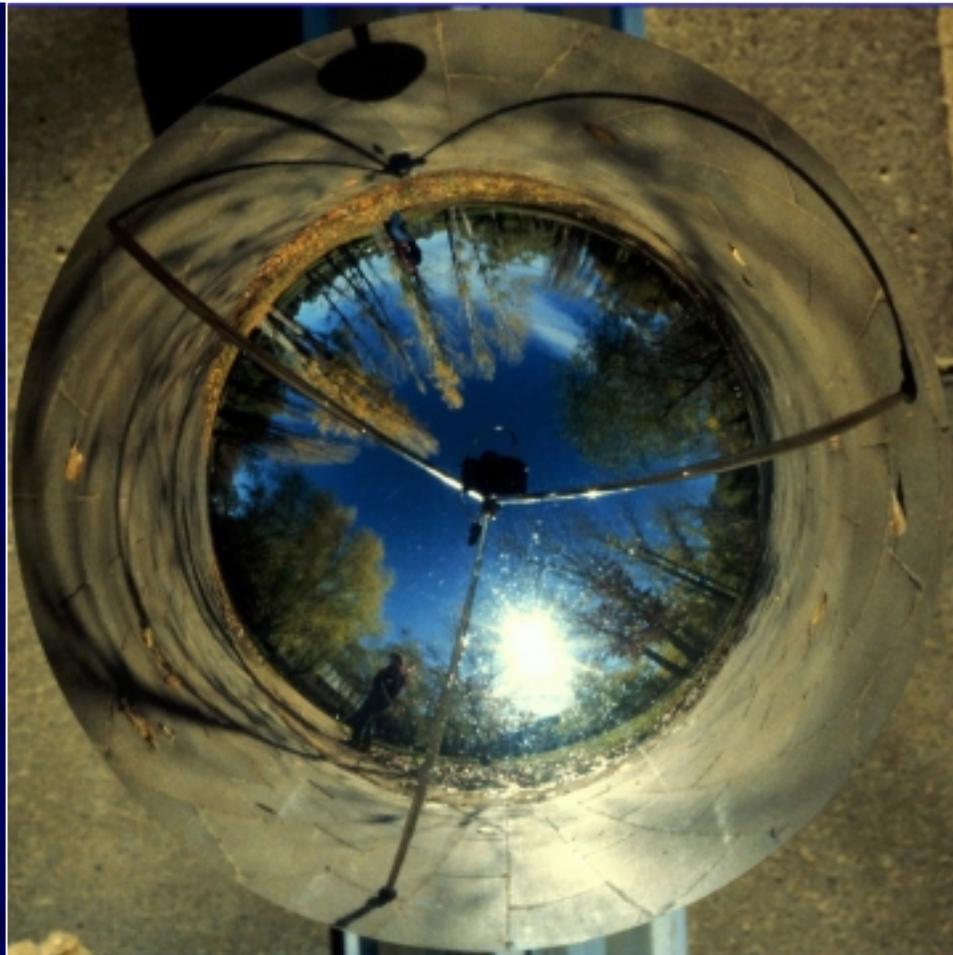
**Generating equation:**

$$\frac{d}{d\theta} \left[ \tan^{-1} \left( r \frac{d\theta}{dr} \right) \right] = \kappa, \quad \text{where } \kappa = -(1 + \alpha) / 2$$

$$\Rightarrow \sin[A - \theta(1 + \alpha) / 2] = (Br)^{(1-\alpha)/2}$$

Constants of integration A and B are set by boundary conditions: distance and slope of surface at  $\theta = 0$ .

Image acquired  
by camera

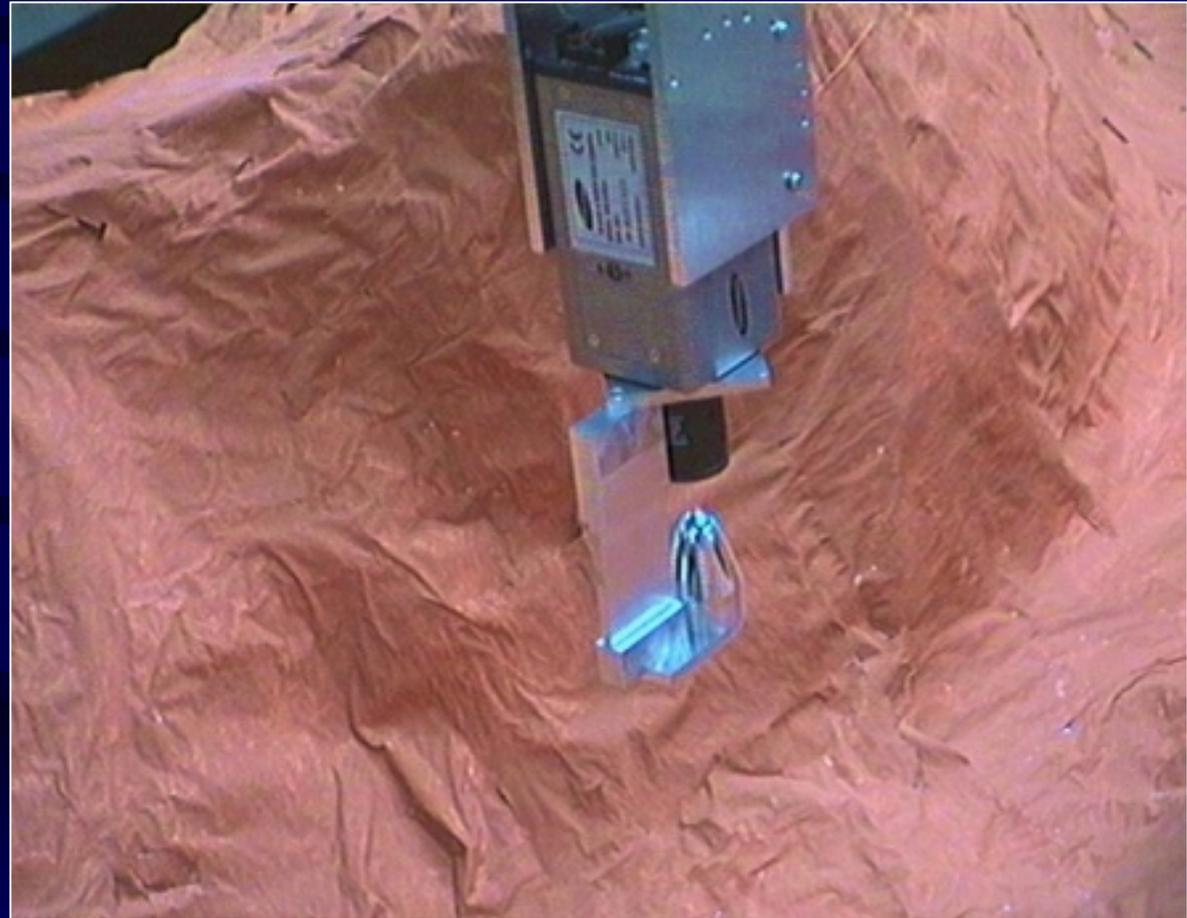


Digitally unwarped  
panoramic image



## Navigation in 3-D

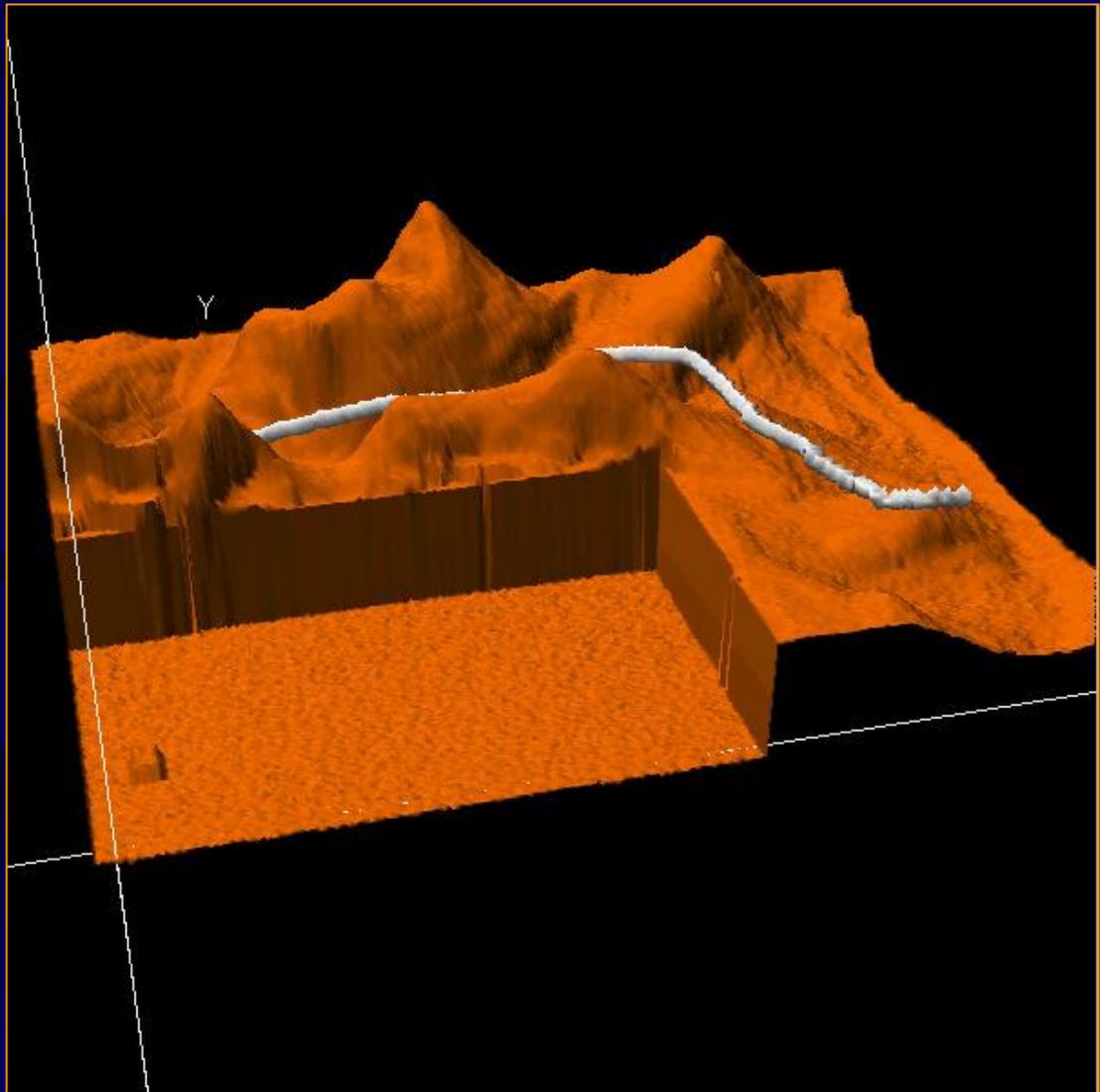
Gantry -based,  
insect-inspired  
navigation system  
emulates flight in  
realistic terrain



## Navigation in 3-D(contd.)

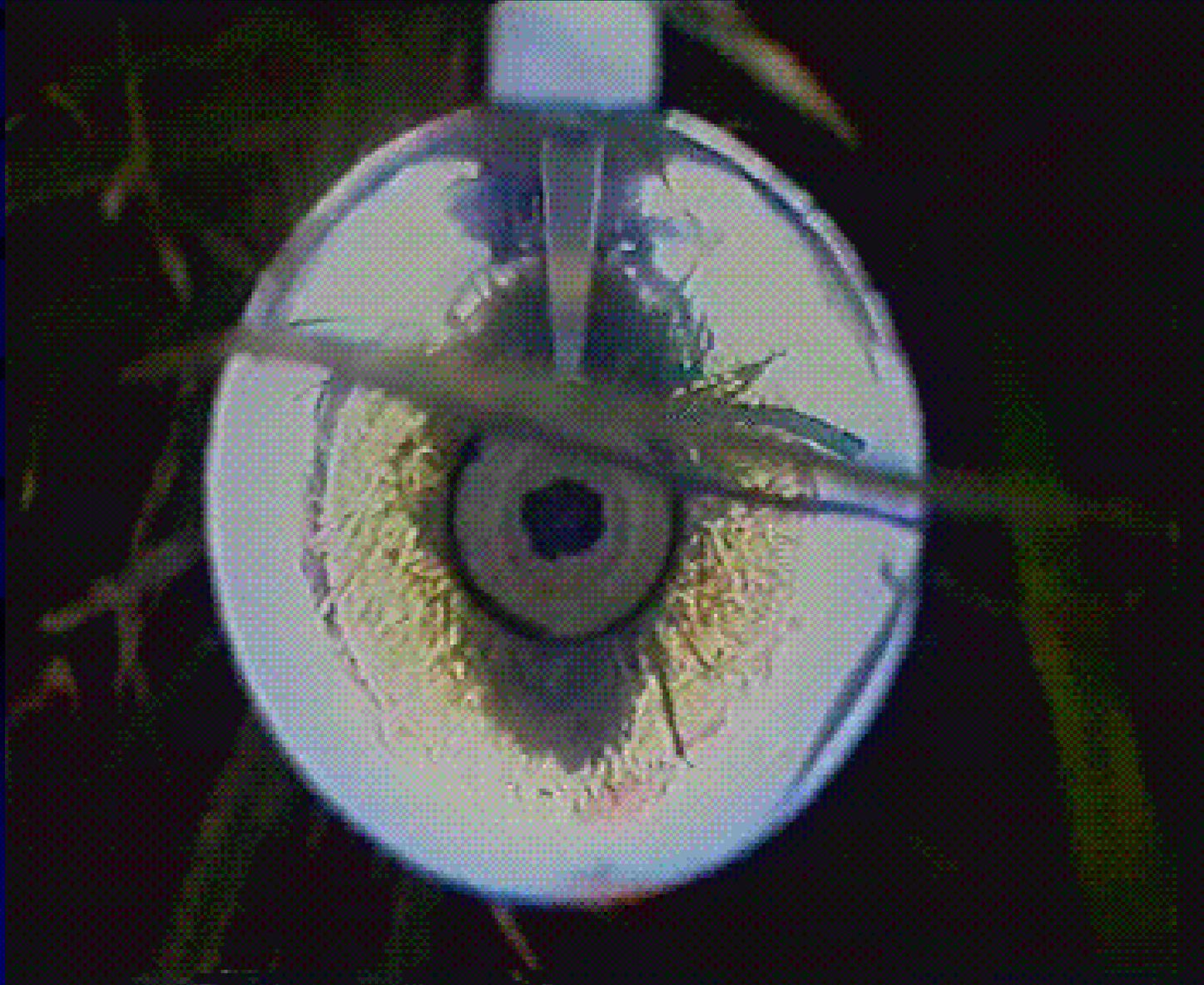
Development and testing of algorithms for landing, terrain following, gorge following, obstacle avoidance and point-to-point navigation

Chahl & Srinivasan (2000b)





# Panoramic video imaging from a helicopter



# Summary

1. Principles of insect vision and navigation
2. Applications to robotics



# Colleagues and collaborators

## 1. Insect vision

Monika Altwein

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Klaus Bartsch

University of Tübingen

K. Chandrashekara

Indian Institute of Science

Ken Cheng

Macquarie University

Tom Collett

University of Sussex

Andrew Giger

Australian National University

Adrian Horridge

Australian National University

Wolfgang Kirchner

University of Konstanz

Miriam Lehrer

University of Zürich

Akiko Mizutani

Australian National University

Jürgen Tautz

University of Würzburg

Shaowu Zhang

Australian National University

Hong Zhu

Australian National University



# Colleagues and collaborators

## 2. Machine vision & robotics

Erhardt Barth

Technical University of Munich

Javaan Chahl

Australian National University

Martin Nagle

Australian National University

Peter Sobey

Australian National University

Gert Stange

Australian National University

Matt Garratt

Australian National University

Dean Socol

Australian National University

Svetha Venkatesh

Curtin University

Keven Weber

Curtin University

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Oxford University





Shaowu Zhang



Javaan Chahl



Zhu Hong



Gert Stange

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Dean Soccol



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